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# Electronic Spectra of Atoms

Ron Robertson

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# I. Spin Orbit Coupling

## A. Origin

- **Electron has spin angular momentum and moving charges generate magnetic fields, so an electron has a magnetic moment.**
- **An electron with orbital angular momentum also possesses a magnetic moment.**
- **These interact to give spin-orbit coupling, the magnitude of which depends on the relative orientations of spin and orbital magnetic moments.**

## B. Total Angular Momentum of One Electron

- **Vector sum gives total angular momentum.**
- **Value is  $j = l \pm s$  or  $j = l \pm 1/2$**

- **Quantum mechanical calculations lead to the fact that there are different energies for a particular configuration based on the spin-orbit coupling.**

**Example: What would be the splitting of the spectra resulting from the excited state for the potassium atom  $[\text{Ar}]5p^1$ .**

**Answer: Since  $l=1$  for p level and  $s=1/2$  so  $j=3/2$  and  $1/2$  and the spectra should be split into two lines.**

### **C. Term symbols**

**Term symbols such as  $^2P_{3/2}$  convey the information given above for the spin-orbit interaction.**

**(1) The letter (S, P, D) indicates the total orbital angular momentum**

**(2) The left superscript in the term symbol gives the multiplicity of the term**

**(3) The right superscript on the term symbol is the value of the total angular momentum quantum number J**

**We shall now break each one down.**

#### **D. Total Orbital Momentum**

**When several electrons are present, it is necessary to judge how their individual angular momenta add together. The total angular momentum L is obtained by coupling the individual orbital angular momenta. For two electrons:**

$$L = |l_1 - l_2| \text{ to } l_1 + l_2$$

- Example: For two p electrons,  $L = 2, 1, 0$ . Hence a  $p^2$  configuration can give rise to D, P and S terms. They differ in energy on account of the different electrostatic interactions between the electrons arising from their different orbital occupations.**

- **Example:** For three electrons we use two series in succession – first we couple two electrons, and then we couple the third to each combined state. For a  $p^2$  we have  $L' = 2, 1, 0$  so we couple the third electron to each of these states. With  $L'=2$  we get  $L=3, 2, 1$ ; with  $L' = 1$  we get  $L=2, 1, 0$ ; with  $L'=0$  we get  $L=1$ . The overall result is  $L=3, 2, 2, 1, 1, 1, 0$ ; one F state, two D states, three P states and one S state.
- Remember that what we are doing is getting the vector sum of the angular momenta!

#### D. Multiplicity

When there are several electrons to be taken into account, we must assess the total spin angular momentum  $S$ . For two electrons:

$$S = |s_1 + s_2| \text{ to } |s_1 - s_2|$$

- **Example:** For two electrons,  $S = 1, 0$ .

- **Example:** For three electrons, couple the third electron to the  $S$  values of the first two. Thus  $S = 3/2$  and  $1/2$  from coupling the third electron to  $S'=1$ , and  $S = 1/2$  from coupling the third electron to  $S'=0$ .

The multiplicity of a term is the value of  $2S + 1$ . When  $S = 0$  (as for a closed shell) the electrons are all paired and there is no net spin: this gives a singlet term, such as  $^1S$ . [Try not to confuse the  $S$  of the term symbol with the  $S$  for the total spin angular momentum – it's very difficult to keep them straight in the beginning] A single electron gives rise to a double term such as  $^2S$ . With two unpaired electrons,  $S=1$  and the multiplicity is 3.

## **E. Total Angular Momentum and Russell-Saunders Coupling**

**The total angular momentum quantum number  $j$  tells us the relative orientation of the spin and orbital angular momenta of a single electron. The total angular momentum  $J$  does the same for several electrons. If there is a single electron outside a closed shell then  $J=j$ .**

**Example: The  $[\text{Ne}]3p^1$  configuration has  $l=1$  and therefore  $j=3/2$  and  $1/2$ ; the  $^2P$  term has two levels,  $^2P_{3/2}$  and  $^2P_{1/2}$ .**

**If there are several electrons outside a closed shell we have to consider the coupling of all the spins and all the orbital angular momenta. This is a nasty problem that can be simplified by the use of the Russell-Saunders coupling scheme.**

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# Russell Saunders Coupling

We imagine that all the orbital angular momenta of the electrons couple to give some total  $L$  and that all the spins are similarly coupled to give some total  $S$ . Only then do we imagine the momenta coupling through the spin-orbit interaction. The permitted values of  $J$  are:

$$J = |L-S| \text{ to } L + S$$

For the  $^3D$  term of the configuration  $[\text{Ne}]2p^13p^1$ , the permitted values of  $J$  are 3,2,1 because  $L=2$  and  $S=1$ . This gives three levels,  $^3D_3$ ,  $^3D_2$ , and  $^3D_1$ .

## A. How to determine term symbols

- Write the configurations but ignore inner closed shells.
- Couple the orbital momenta to find L.
- Couple the spins to find S.
- Couple L and S to find J.
- Express the term as  $^{2S+1}\{L\}_J$ , where L is the appropriate letter.

**Example:** Find the term symbol for the ground configuration of Na. Answer  $^2S_{1/2}$ .

**Example:** Find the term symbols for the configuration of  $2s^1 2p^1$ . Answer  $^3P_2, ^3P_1, ^3P_0, ^1P_1$ .

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# Selection Rules

Spectral transitions can be specified using term symbols. For example, the transitions giving rise to the yellow sodium doublet are:



We have seen that selection rules arise from the conservation of angular momentum during a transition and from the fact that a photon has a spin of 1. They can be expressed in terms of the term symbols, because the latter carry information about angular momentum.

$$\Delta S = 0 \quad \Delta L = 0, \pm 1 \text{ with } \Delta l = \pm 1$$

$$\Delta J = 0, \pm 1 \text{ but } J = 0 \text{ cannot combine with } J = 0.$$

The rule about  $\Delta S = 0$  stems from the fact that light does not affect the spin directly. The rule about  $\Delta L$  and  $\Delta l$

**expresses the fact that the orbital angular momentum of an individual electron must change (so  $\Delta l = \pm 1$ ), but whether or not this results in an overall change of orbital momentum depends on the coupling.**

**These rules are applicable to light atoms. In very heavy atoms the rules may not apply for all transitions as other coupling comes into play.**

